

# Permeability Studies Applied to Grain Boundary Diffusion in Alumina Scales

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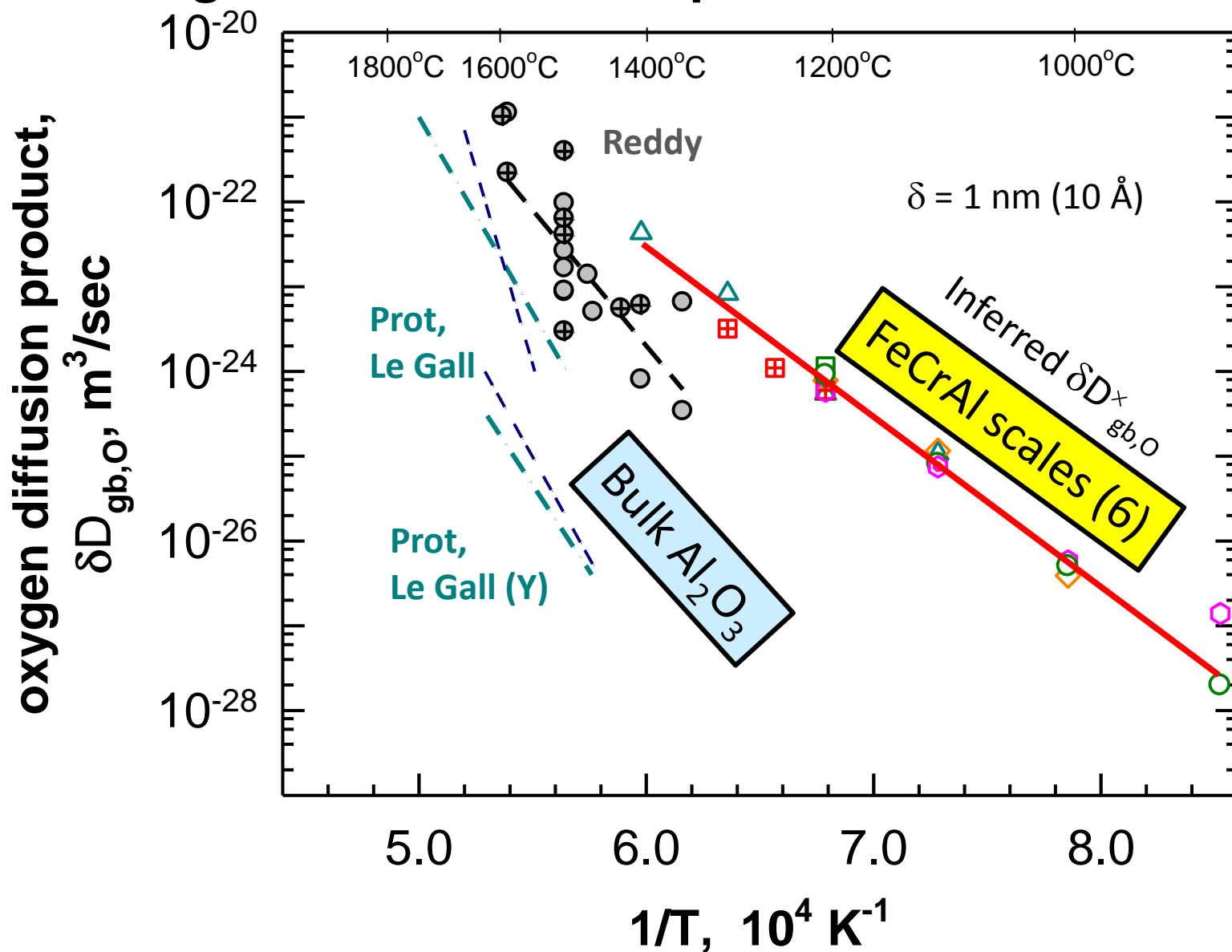
# Alumina Scale Growth Mechanisms: Signposts along a 40 year journey

1. **Bulk**  $\text{Al}_2\text{O}_3$  vs  $\text{Al}_2\text{O}_3$  **scale** diffusivity
2. **Oxygen** inward vs **Aluminum** outward ( n-type vs p-type)
3. Short circuit **grain boundary** diffusion (grain growth)
4. 'cubic' or **sub-parabolic** growth rates
5.  $^{18}\text{O}$  **tracer** (double oxidation) studies (NRA, SIMS profiles)
6. **Activation energies** (Arrhenius plots of  $\log k_p$  vs  $1/T$ )
7. Growth **stress**; creep relaxation
8. **Dopant** effects on defects, transport, and morphology
9.  $p\text{O}_2$  effects on  $\sigma_{el}$ ,  $\sigma_l$ ,  $[V_O^{\circ\circ}]$ ,  $[V_{Al}''']$ ,  $D_O$ ,  $D_{Al}$

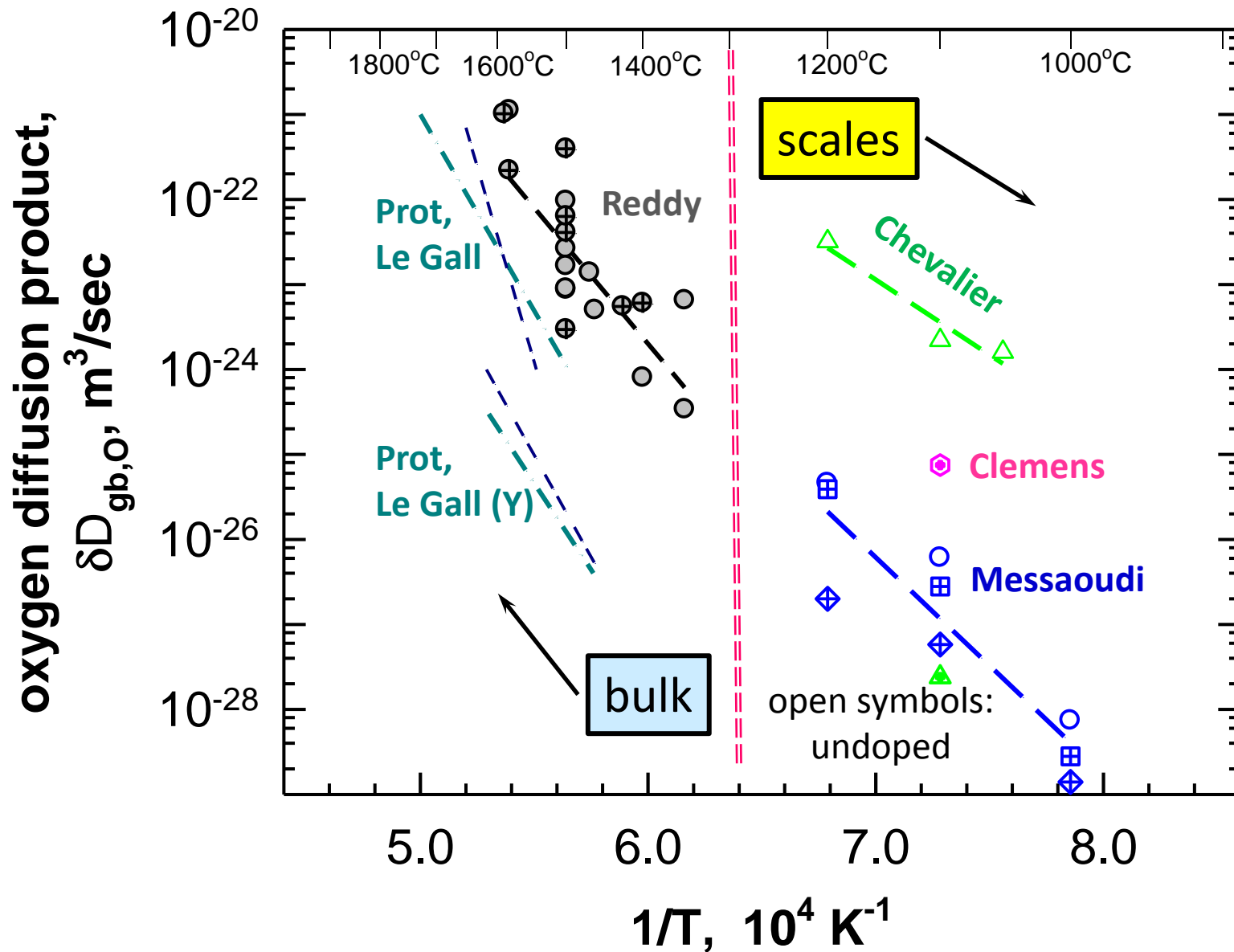
# Objectives

- Introduce permeability,  $\delta D_{gb,O,Al}$  equations
- New Wagner solutions
- Compare  $k_{p,i}$  (predicted, measured, literature)
- Compare  $\delta D_{gb,O}$   
predicted: permeability vs oxidation  
measured:  $^{18}O$  literature)
- Recap, new insights
- Epilogue: MDC150L Ni(Pt)Al coating

# Alumina Grain Boundary Diffusivity Product Wagner Oxidation Compared to Bulk<sup>18</sup>O Tracer



# Alumina Grain Boundary Diffusivity Product <sup>18</sup>O Tracer: Bulk Compared to Oxidation



# Wagner Model (from Kofstad)

$$k_{p,\text{instant}} = 2x \frac{dx}{dt} = \int_{P_{O_2,\text{interface}}}^{P_{O_2,\text{gas}}} \left( \frac{3}{2} D_{\text{eff},Al} + D_{\text{eff},O} \right) d \ln P_{O_2}$$

**GOAL:  $k_p \leftrightarrow D_{Al, O} (Al_2O_3)$**

## Grain Size Affects $D_{\text{eff}}$

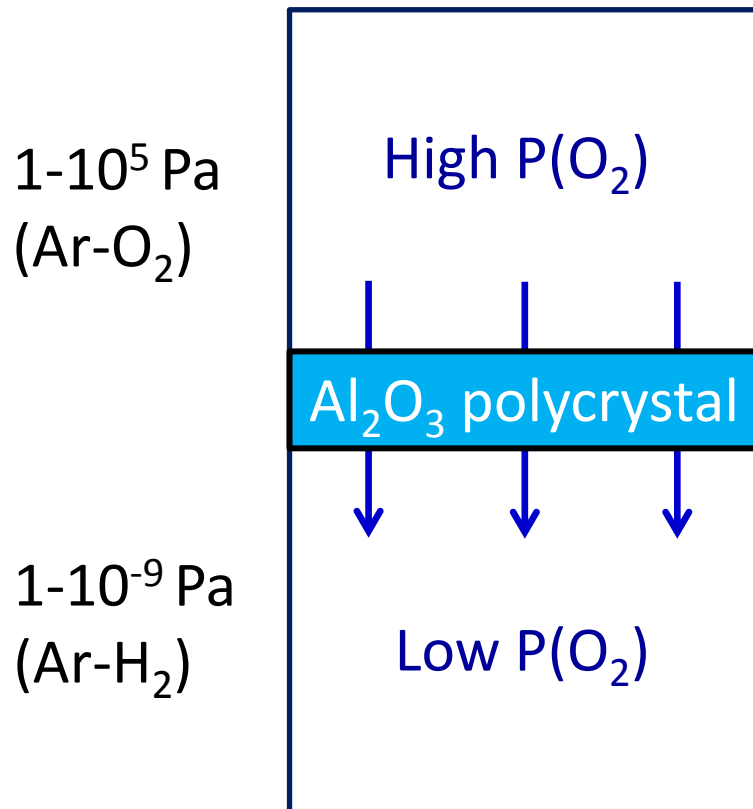
$$D_{\text{eff}} = (1 - f)D_l + f(D_{gb})$$

$$D_{\text{eff}} \approx fD_{gb} = \frac{2\delta D_{gb}}{G_i}$$

$$G_i \text{ (grain size)} \propto T, t$$

# Alumina Permeability Studies:

Wada, Matsudaira, Kitaoka; JCS-Japan 119 (2011) 832-839



Vary I or II

Measure P(H<sub>2</sub>O)

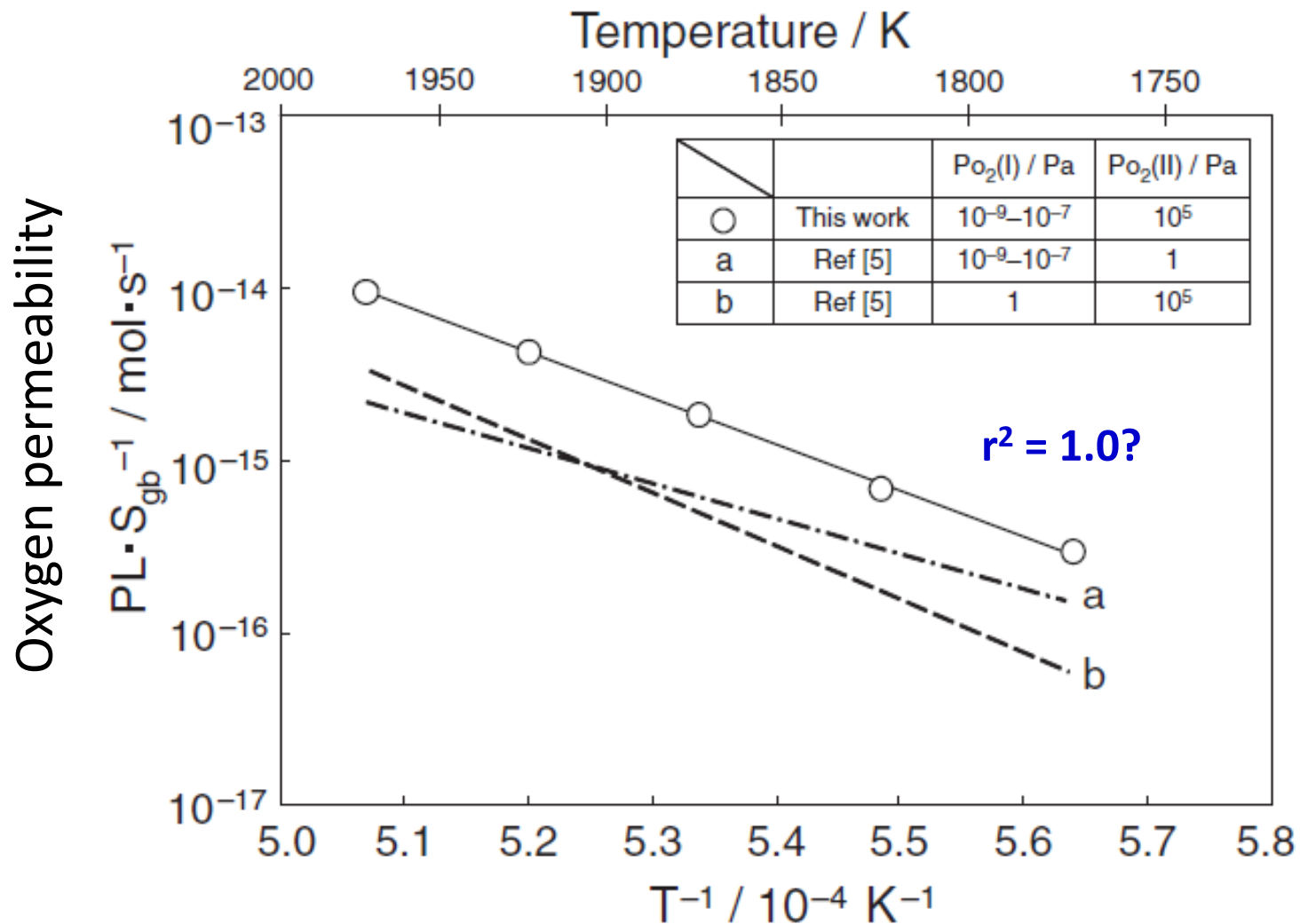
Measure P(O<sub>2</sub>)

Calculate  $P, J, \mu_O, \delta D_{gb}$   
(vs depth!)



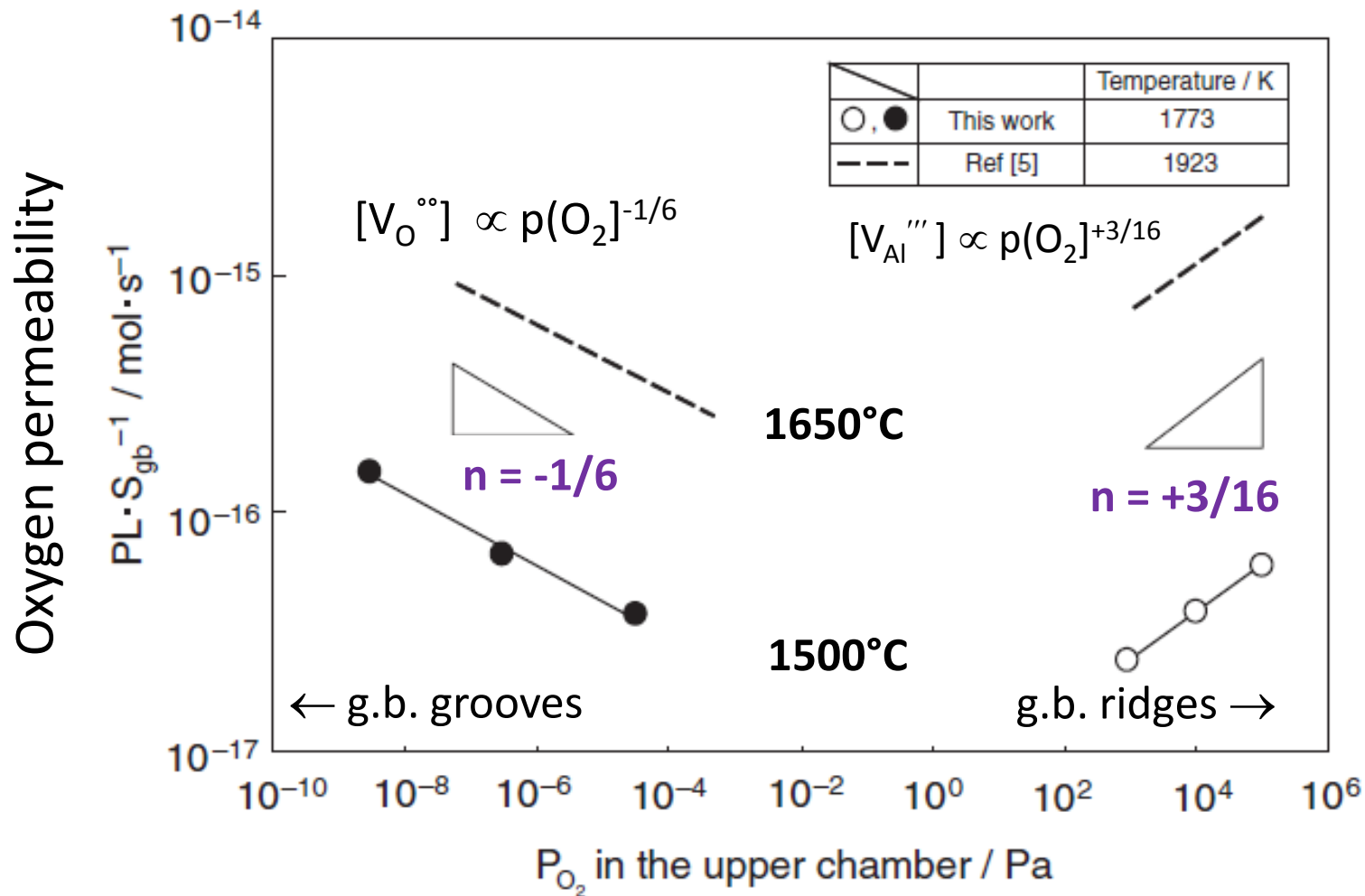
# Alumina Permeability Studies: Temperature Effects

Wada, Matsudaira, Kitaoka; JCS-Japan 119 (2011) 832-839



# Alumina Permeability Studies: $P(O_2)$ Effects

Wada, Matsudaira, Kitaoka; JCS-Japan 119 (2011) 832-839



$\delta D_{gb}$  Measured from Alumina Permeability Studies

Wada, Matsudaira, Kitaoka; JCS-Japan 119 (2011) 832-839:

$$\delta D_{gb,O} = 2.207 \times 10^{-9} \exp \left( \frac{-467 \text{ kJ}}{RT} \right) (P_{O_2,low})^{-1/6} \text{ m}^3 / \text{s}$$

$$\delta D_{gb,Al} = 2.475 \times 10^{-5} \exp \left( \frac{-604 \text{ kJ}}{RT} \right) (P_{O_2,high})^{3/16} \text{ m}^3 / \text{s}$$

## Wagner – Permeability Model (Oxygen)

$$k_{p,\text{instant}} = \int_{P_{O_2,\text{interface}}}^{P_{O_2,\text{gas}}} \frac{2A \exp(-Q / RT)}{G_i} P_{O_2}^{-1/6} d \ln P_{O_2}$$

Obtain  $k_{p,i}$ ,  $\delta D_{gb}$  from each other:  
**Oxygen (Primary) Contribution ( $P_{O_2, \text{interface}}$ )**

$$k_{p,i,O} = \frac{12 \delta D_{gb,O, \text{interface}}^{W-W}}{G_i}$$

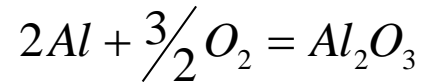
$$\text{or } k_{p,i,O}^{\times} = \frac{2 \delta D_{gb,O}^{\times} \Delta \ln P_{O_2}}{G_i}$$

## Aluminum Contribution ( $P_{O_2, \text{gas}}$ )

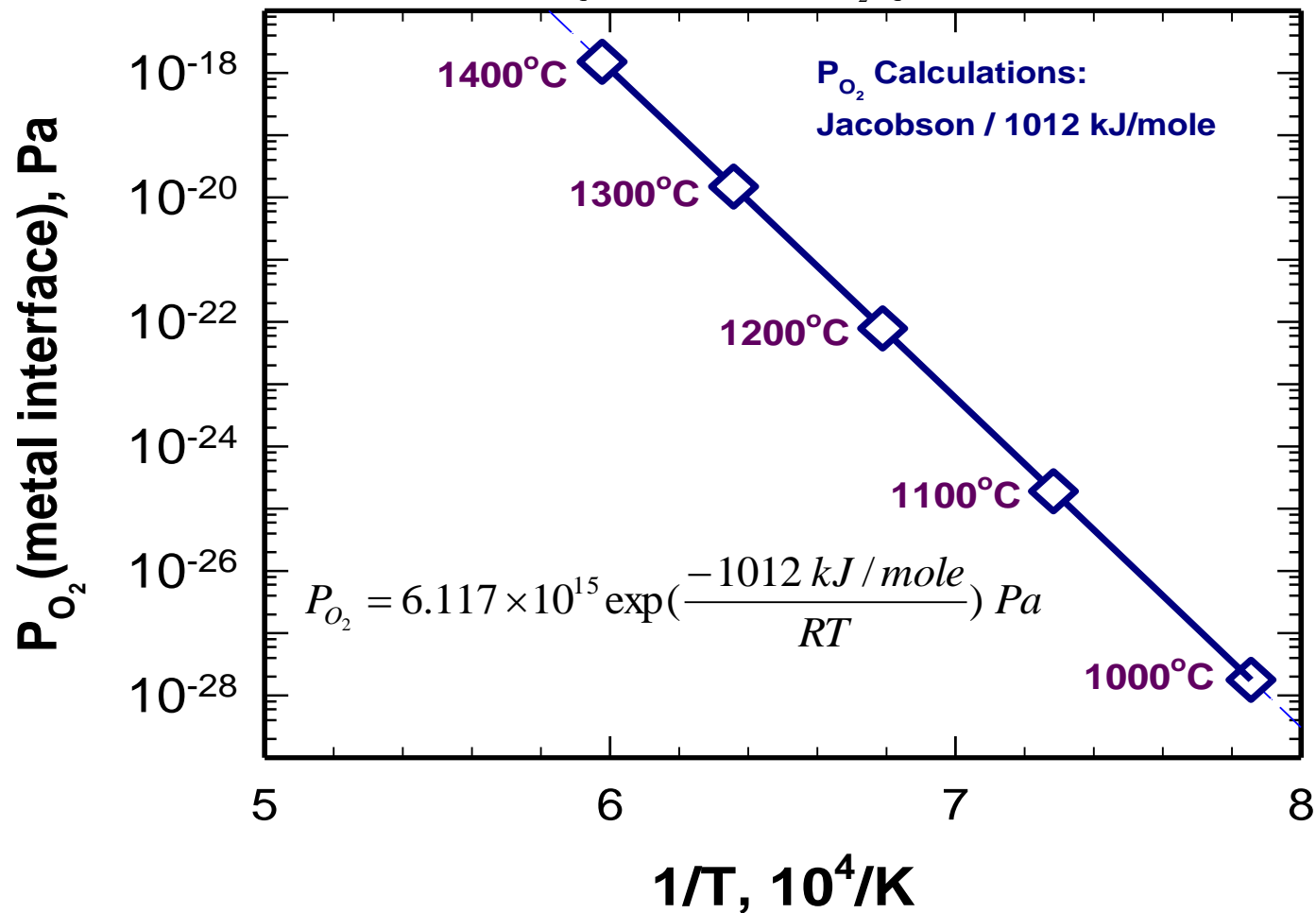
$$k_{p,i,Al} = \frac{16 \delta D_{gb,Al,gas}^{W-W}}{G_i}$$

$$\text{or } k_{p,i,Al}^{\times} = \frac{3 \delta D_{gb,Al}^{\times} \Delta \ln P_{O_2}}{G_i}$$

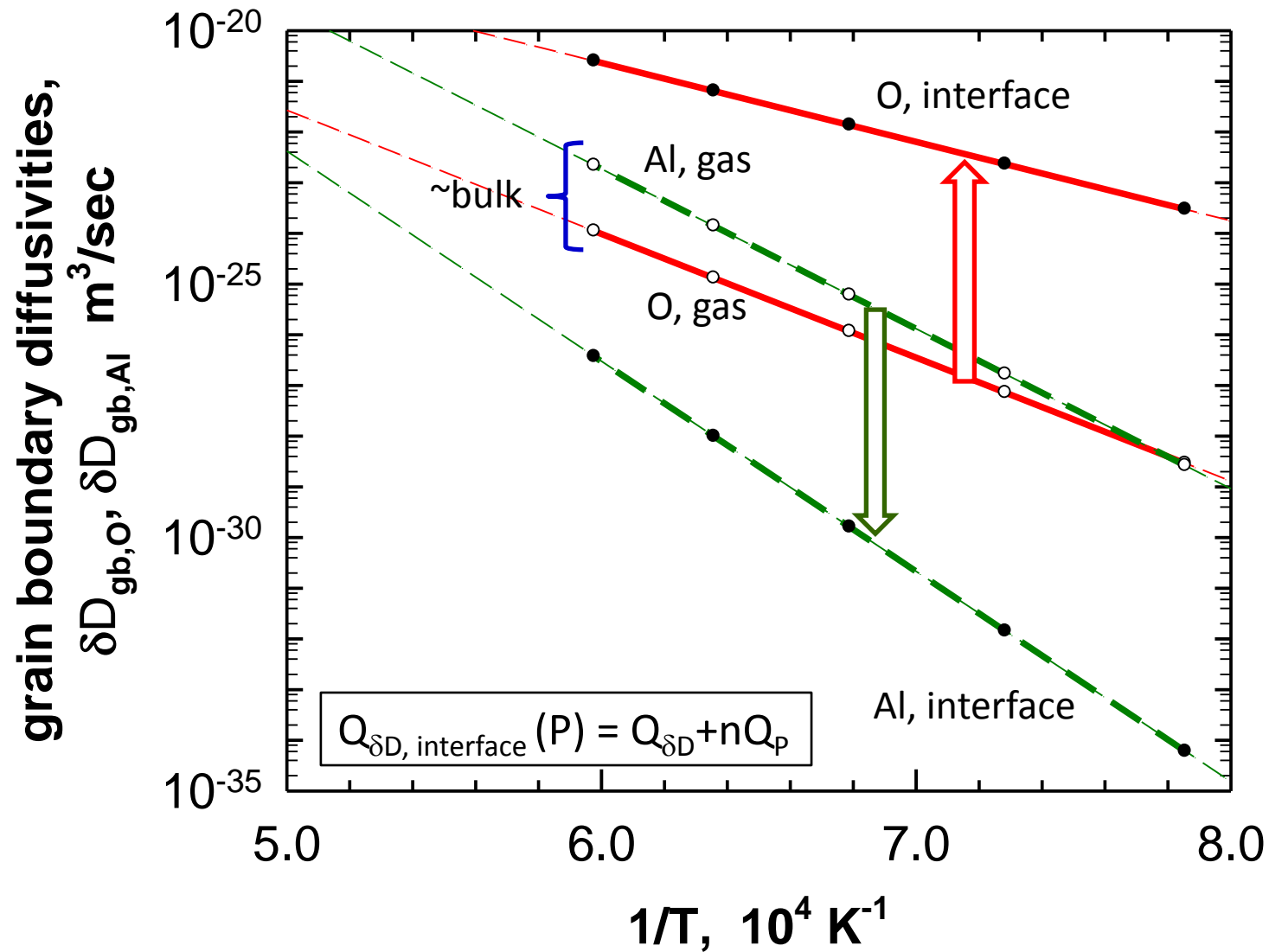
# Equilibrium $P(O_2)$ for FeCrAl(Zr) Oxidation Predictions



$$K_{eq} = 1/(a_{Al})^2(P_{O_2,eqil})^{3/2}$$



# Grain Boundary Diffusivity Product Predictions for FeCrAl Scales vs Bulk Alumina





$$Q_{\delta D \text{ interface}} = Q_{\delta D, \text{ gas}} + nQ_{P,eq}$$

$$Q_{P,eq} = 1012 \text{ kJ/mole}$$

position	$A_i$ (m <sup>3</sup> /s)	$Q_i$ (kJ/mole)	$n_i$
O, gas	4.23E-10	467	-1/6
O, interface	5.16E-12	<b>298</b>	-1/6
Al, gas	1.59E-04	604	+3/16
Al, interface	2.26E-02	<b>794</b>	+3/16

## Measured $k_p$ vs Predicted (Permeability $\delta D_{gb,O}$ )

$$\Pi_i = k_{p,i} \cdot G_i = 12\delta D_{gb,O,interface}$$

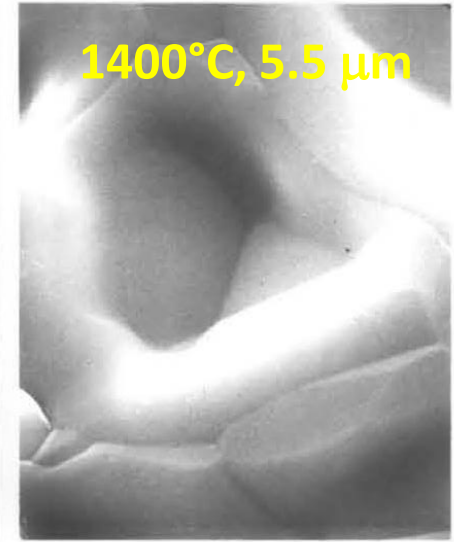
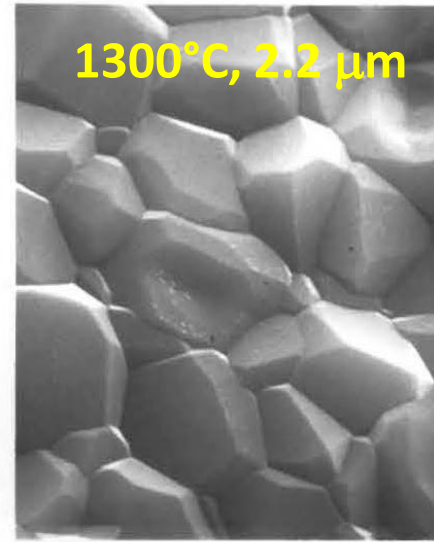
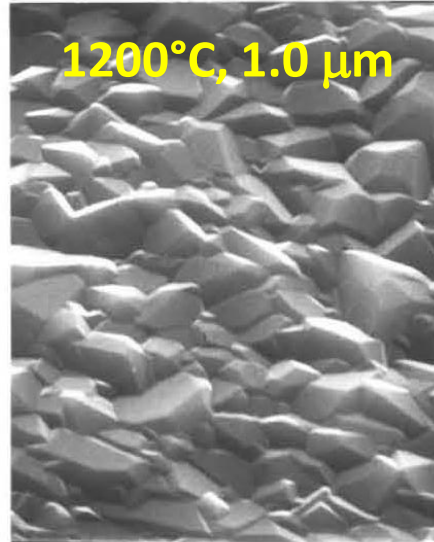
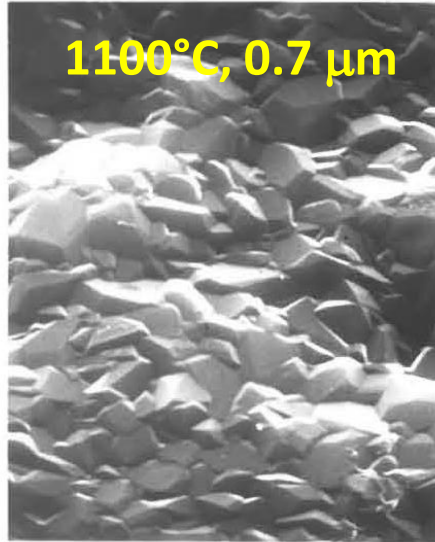
# vs FeCrAl (Zr) Isothermal Oxidation

$x_i$  (mg/cm<sup>2</sup>),  $dx/dt$ ,  $G_i$  for 25 samples

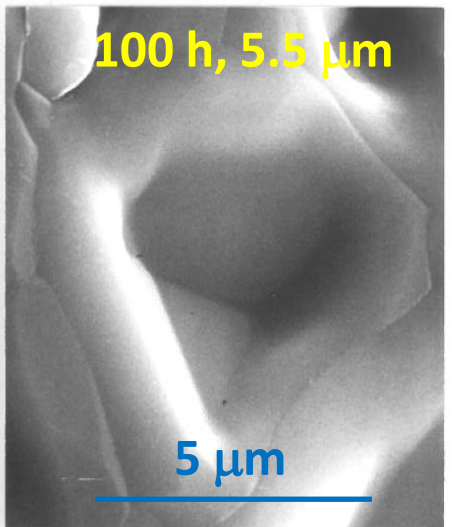
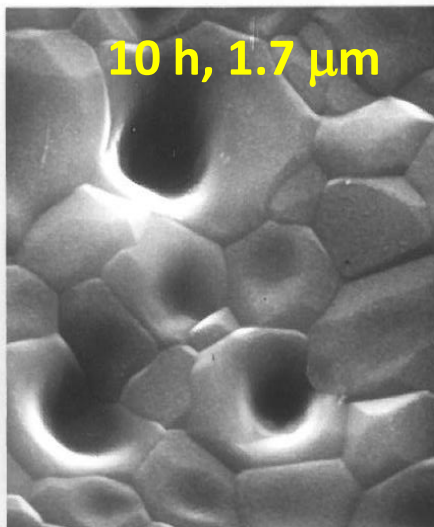
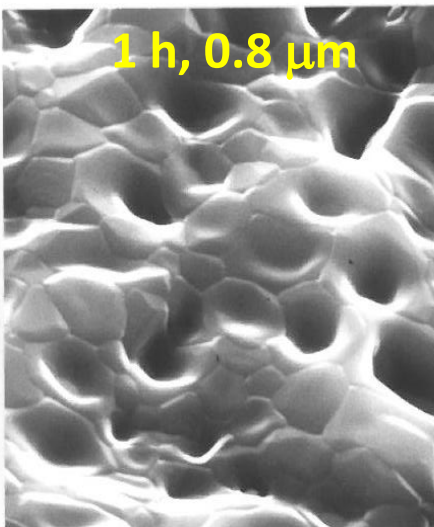
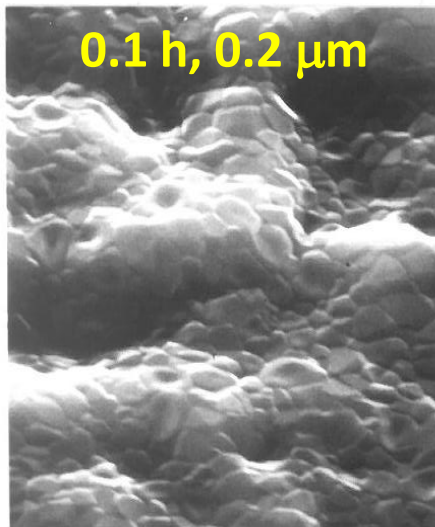
hours	1100°C	1200°C	1300°C	1400°C
0.1				
1				
10				
50				
100				
200				failed
500				
1000			failed	

# $\text{Al}_2\text{O}_3$ Scale Underside Stripped from FeCrAl(Zr)

(A) 100 h

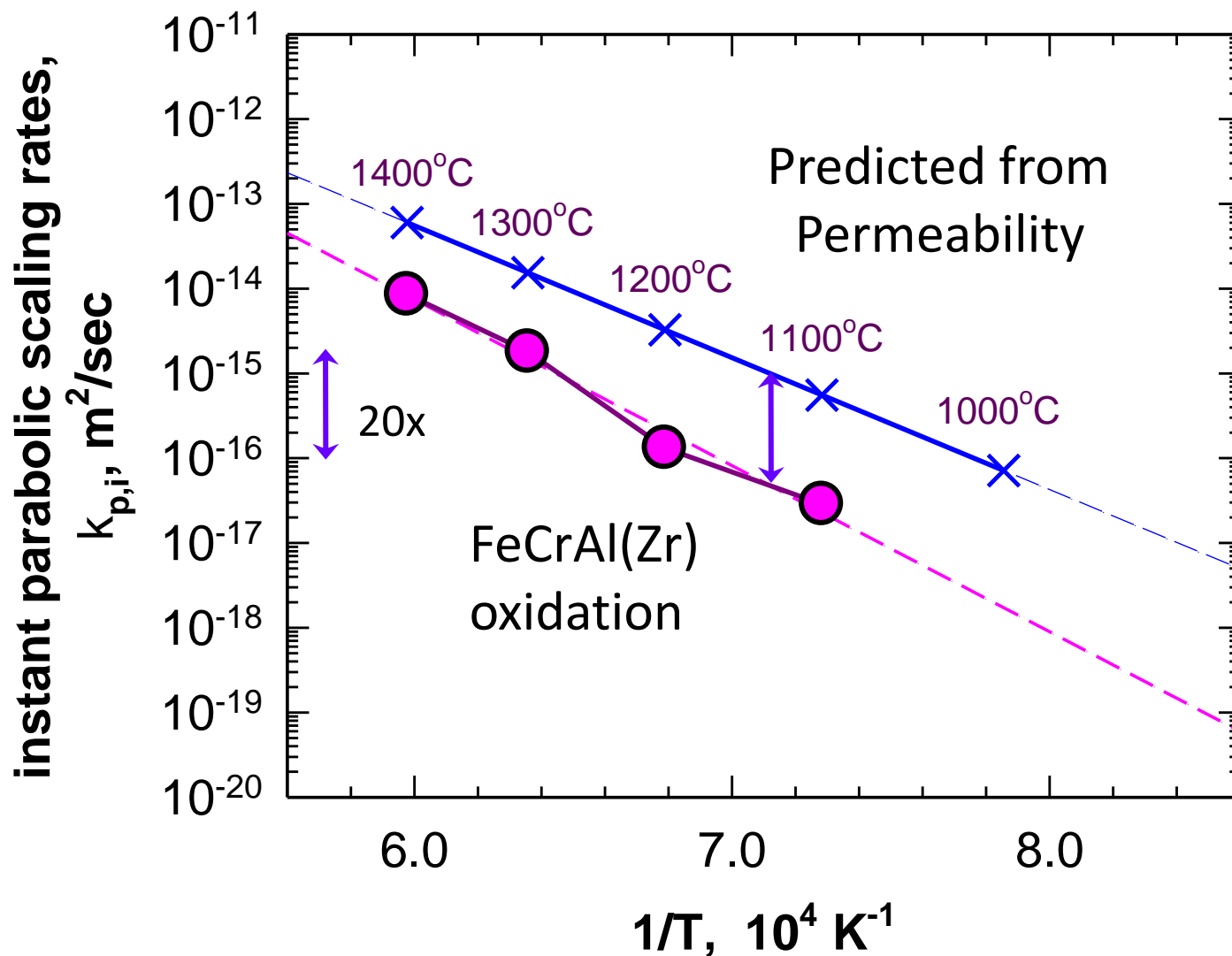


(B) 1400°C,



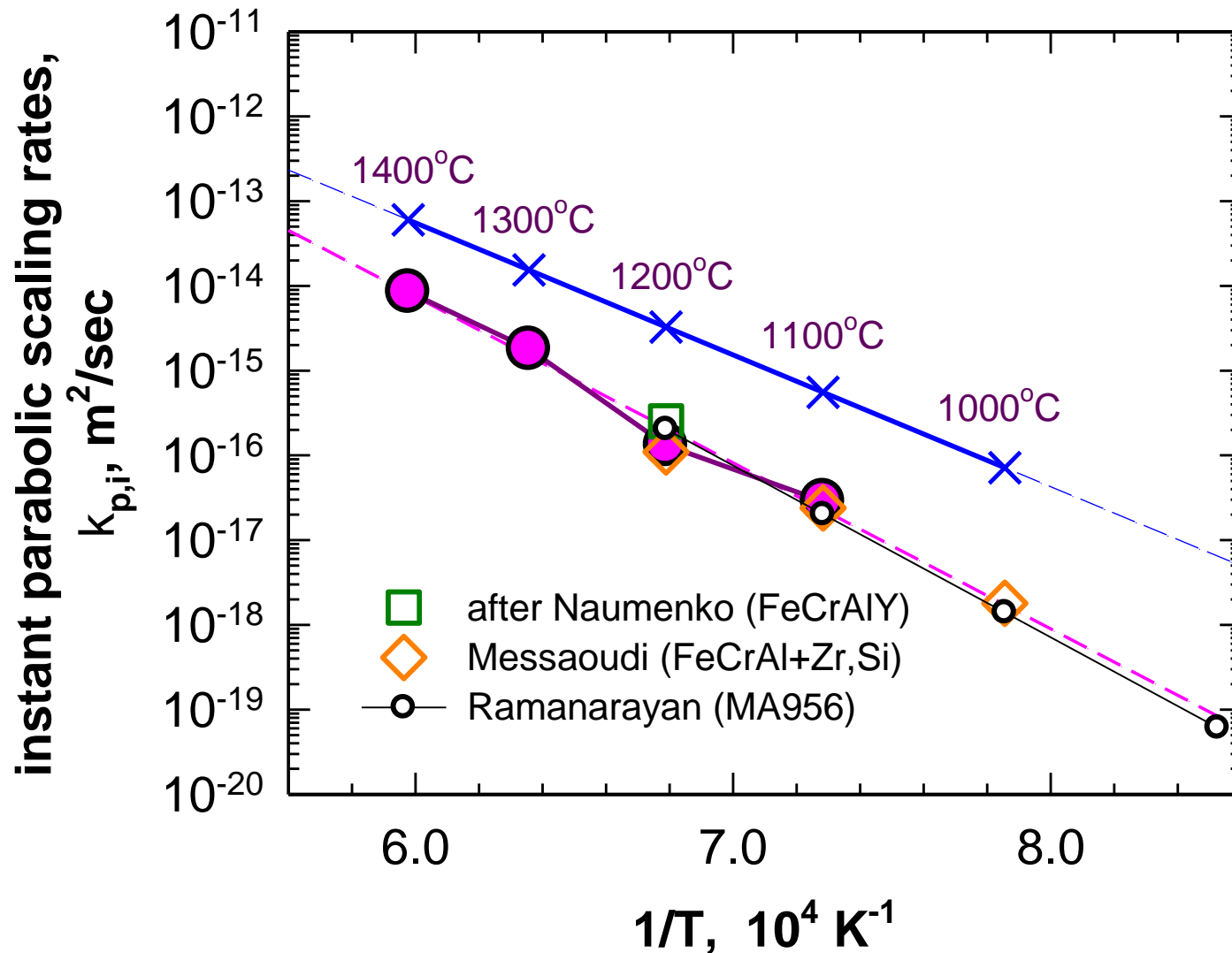
# Alumina Scale Growth Rates on FeCrAl(Zr) $k_{p,i}$ Measured and Predicted from Permeability

$\delta D_{gb,O}$ ;  $k_{p,i}$  at GS = 0.5  $\mu\text{m}$



# Alumina Scale Growth Rates on FeCrAl(Zr) $k_{p,i}$ Measured and Predicted from Permeability

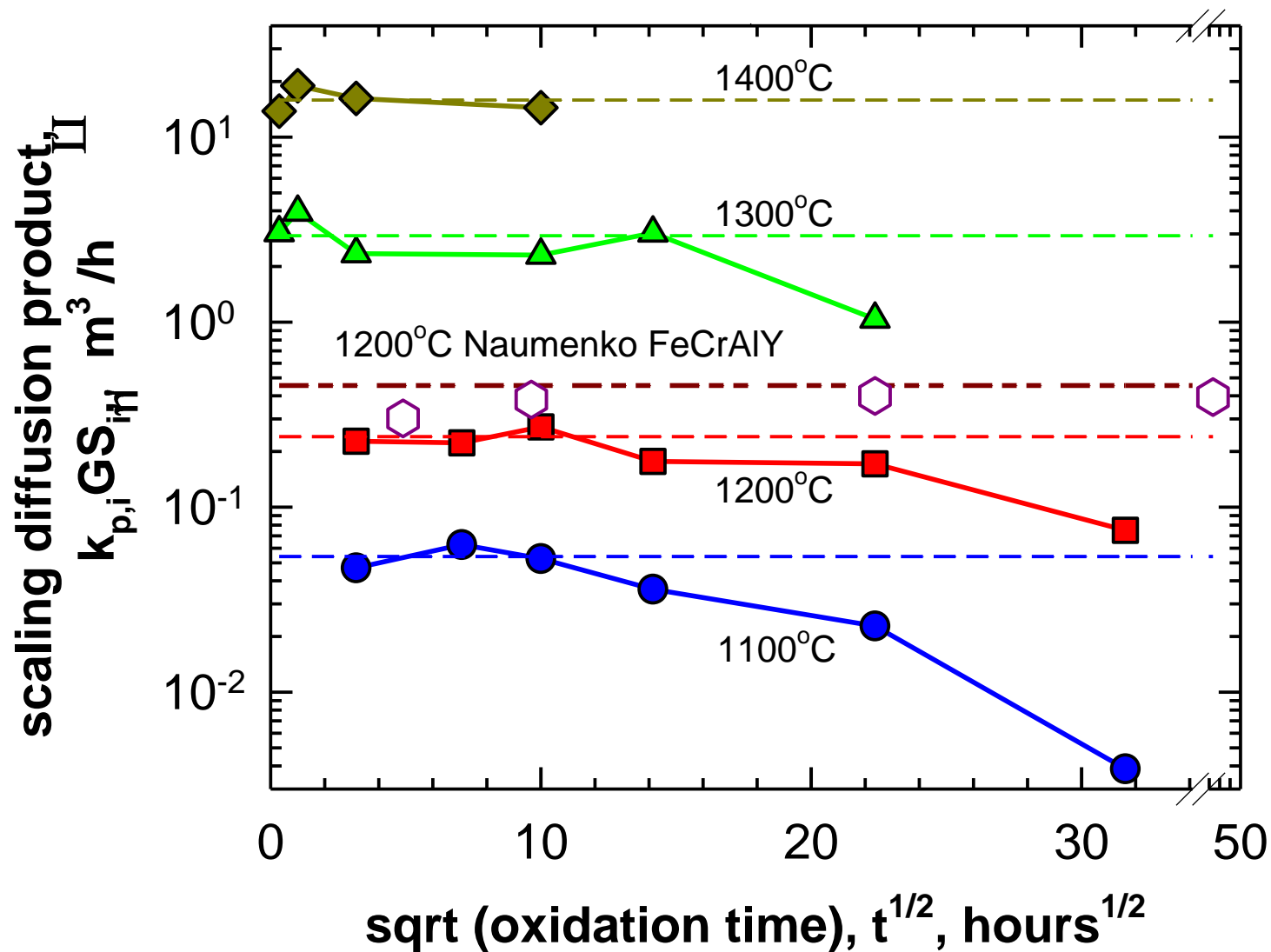
$\delta D_{gb,O}$ ;  $k_{p,i}$  at GS = 0.5  $\mu\text{m}$



**Predict  $\delta D_{\text{gb,O}}$  from  $k_p$**

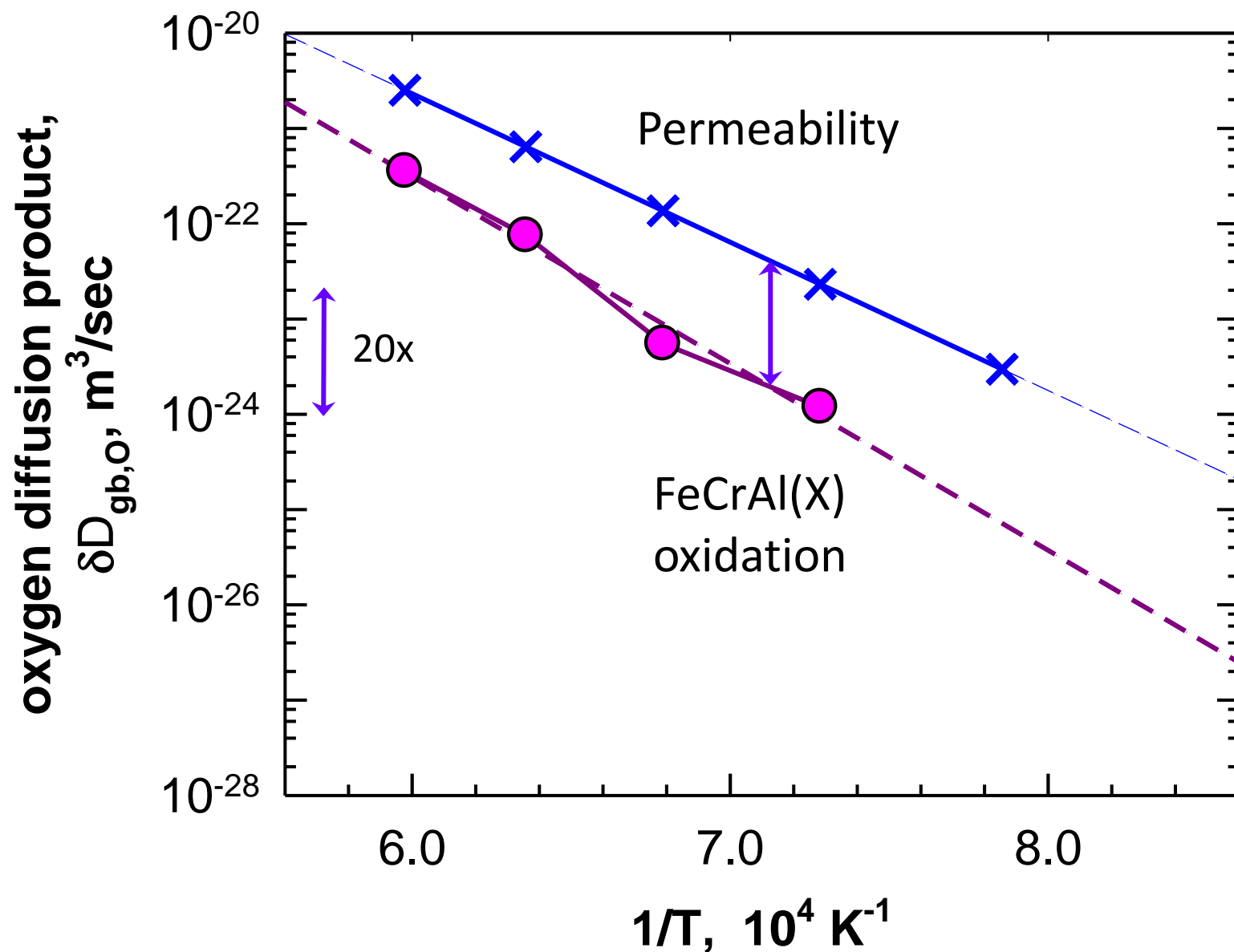
$$\Pi_i = k_{p,i} \cdot G_i = 12\delta D_{\text{gb,O,interface}}$$

# "Invariant" Scaling Product, $\Pi$ , from FeCrAlZr Oxidation Rates

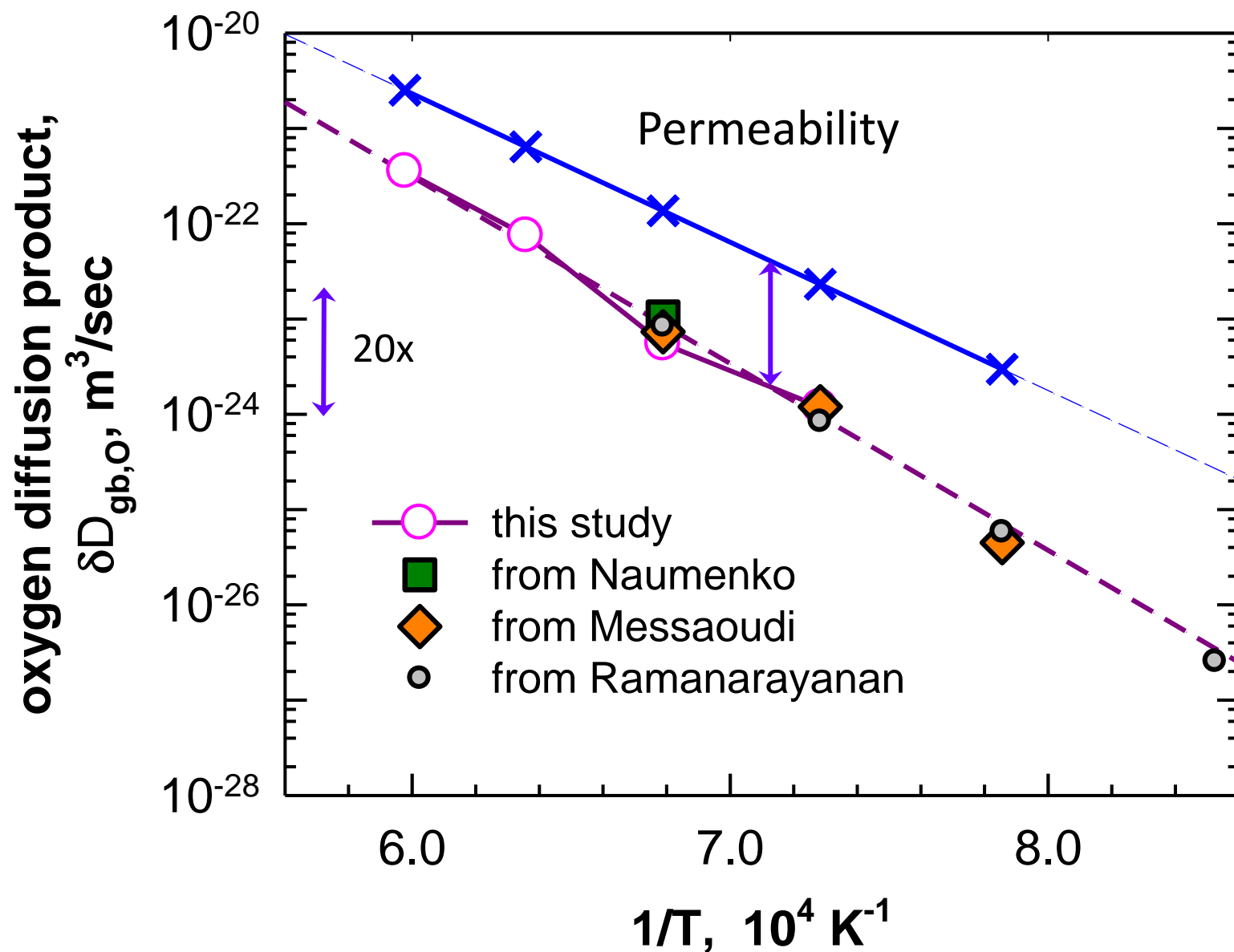




# Scale Grain Boundary Diffusivity Product Oxidation Compared to Permeability Predictions

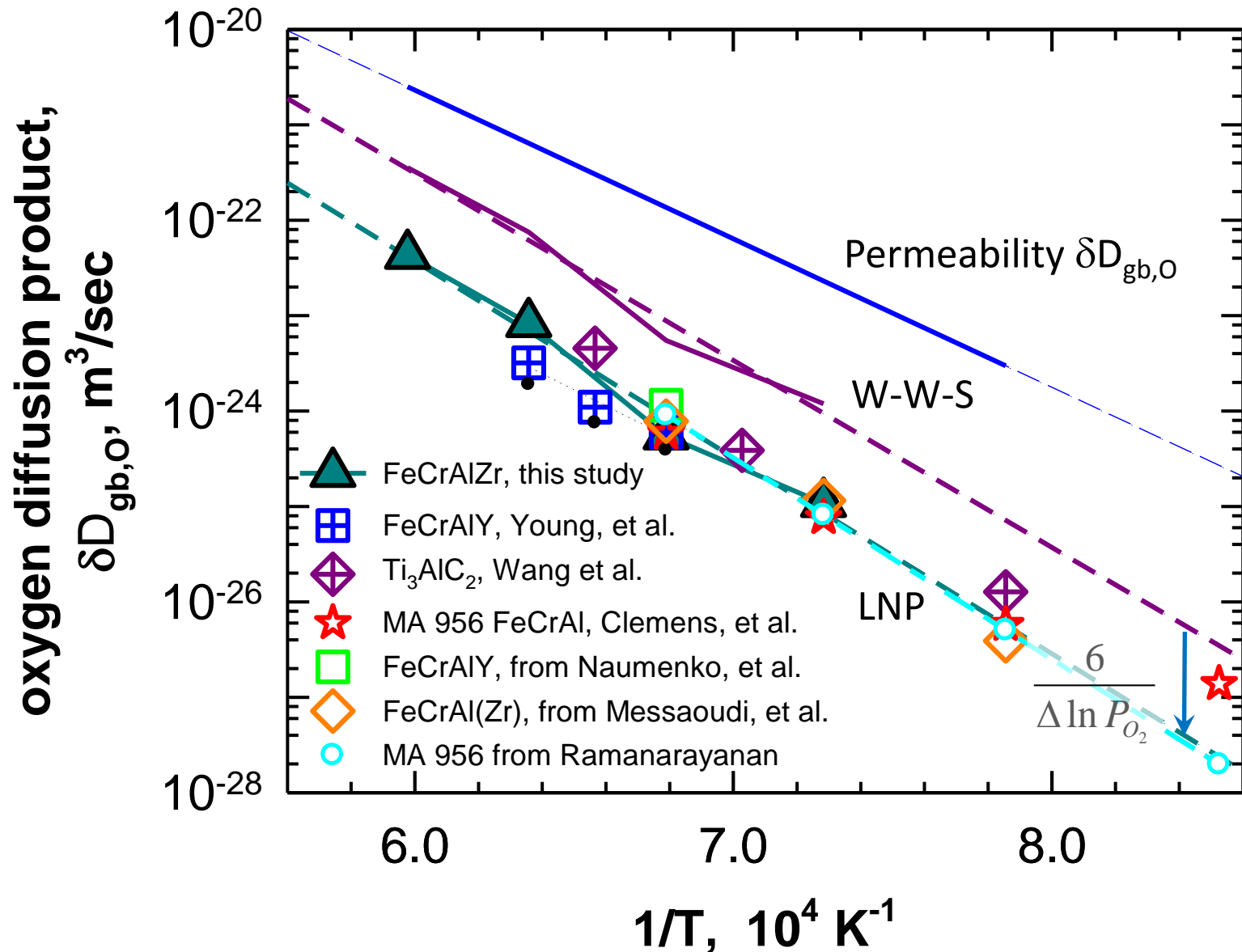


# Scale Grain Boundary Diffusivity Product Oxidation Compared to Permeability Predictions

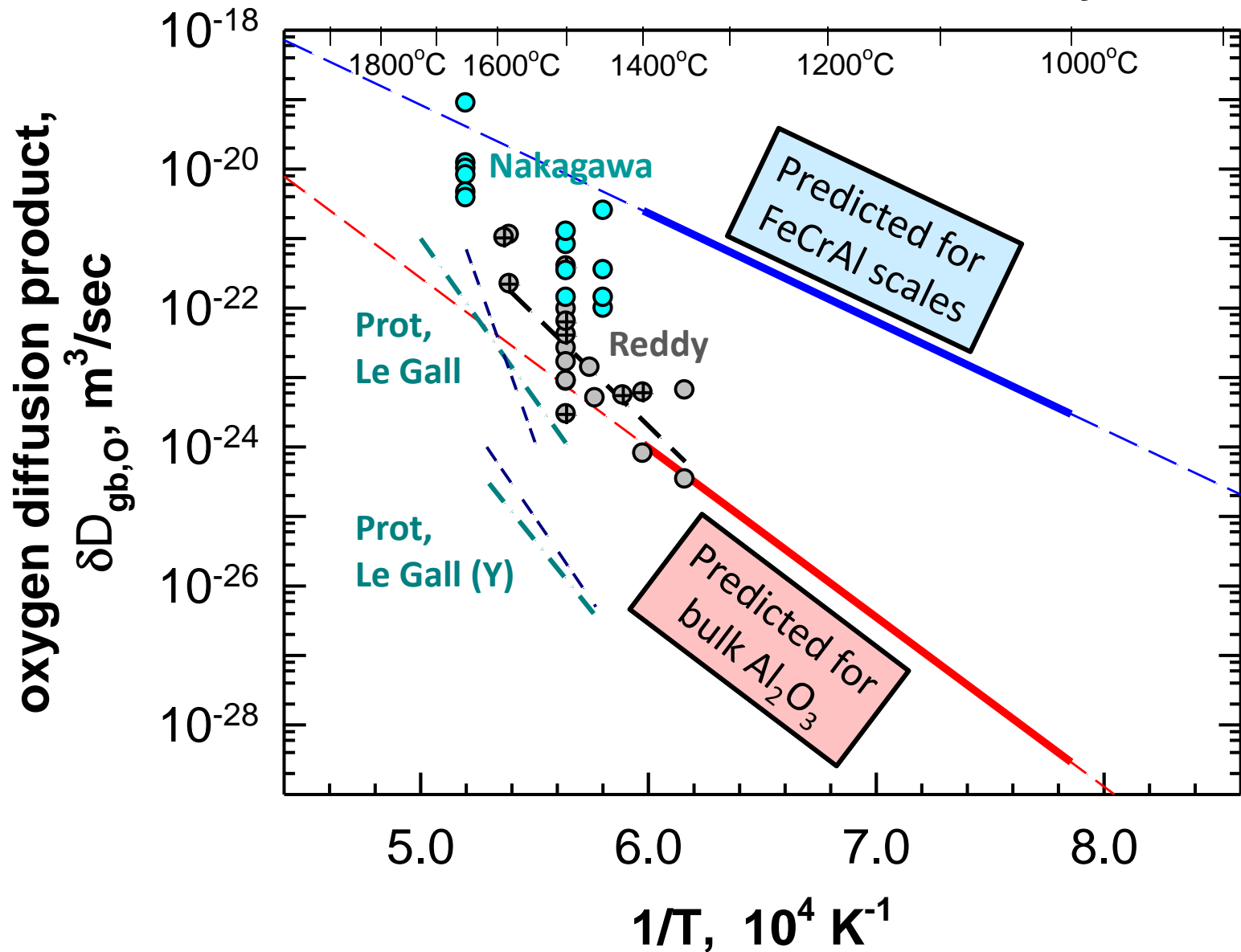


# Scale Grain Boundary Diffusivity Product, $\Delta \ln P_{O_2}$ solution

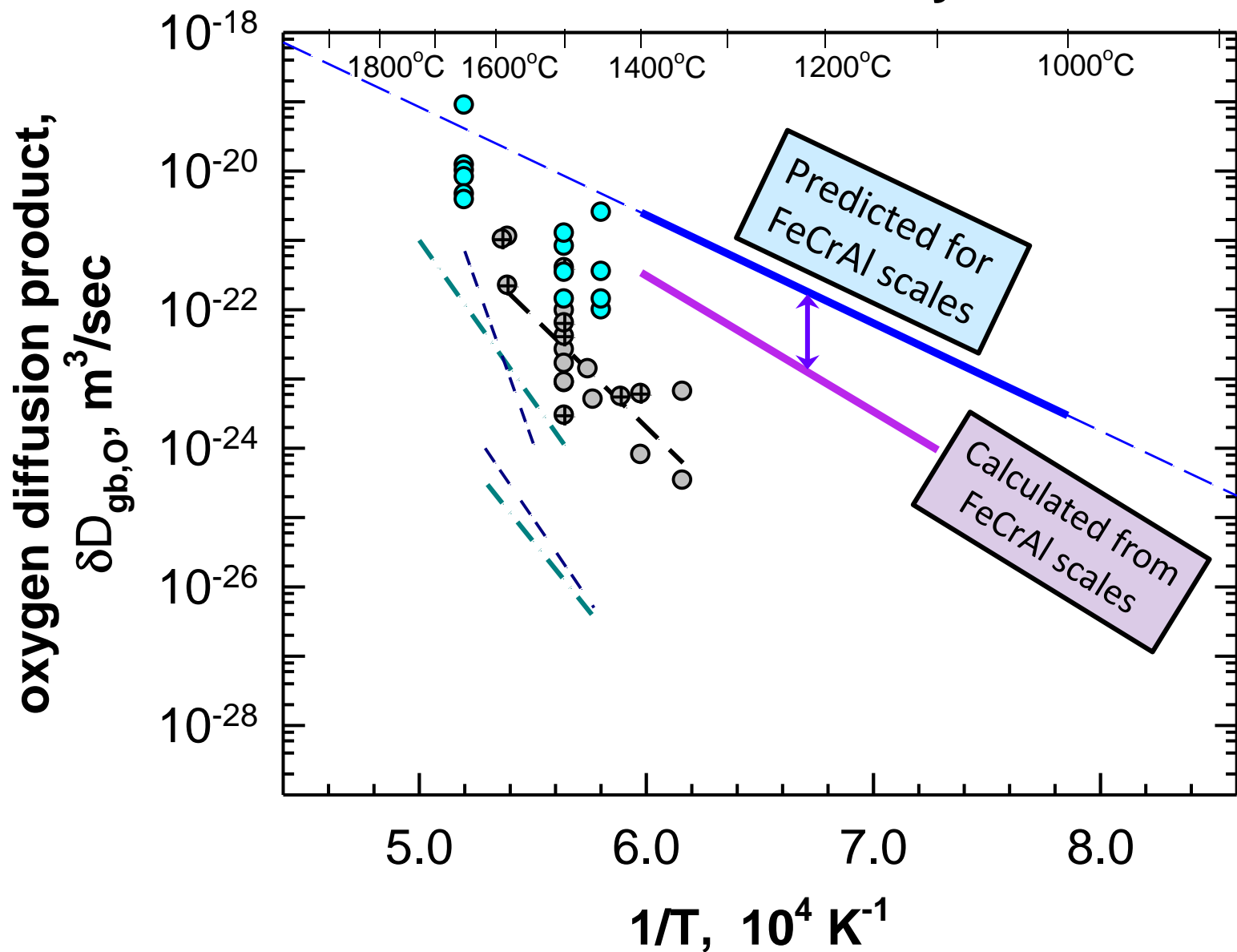
$\delta D_{gb,O}$  from Oxidation (FeCrAl(X),  $Ti_3AlC_2$ )



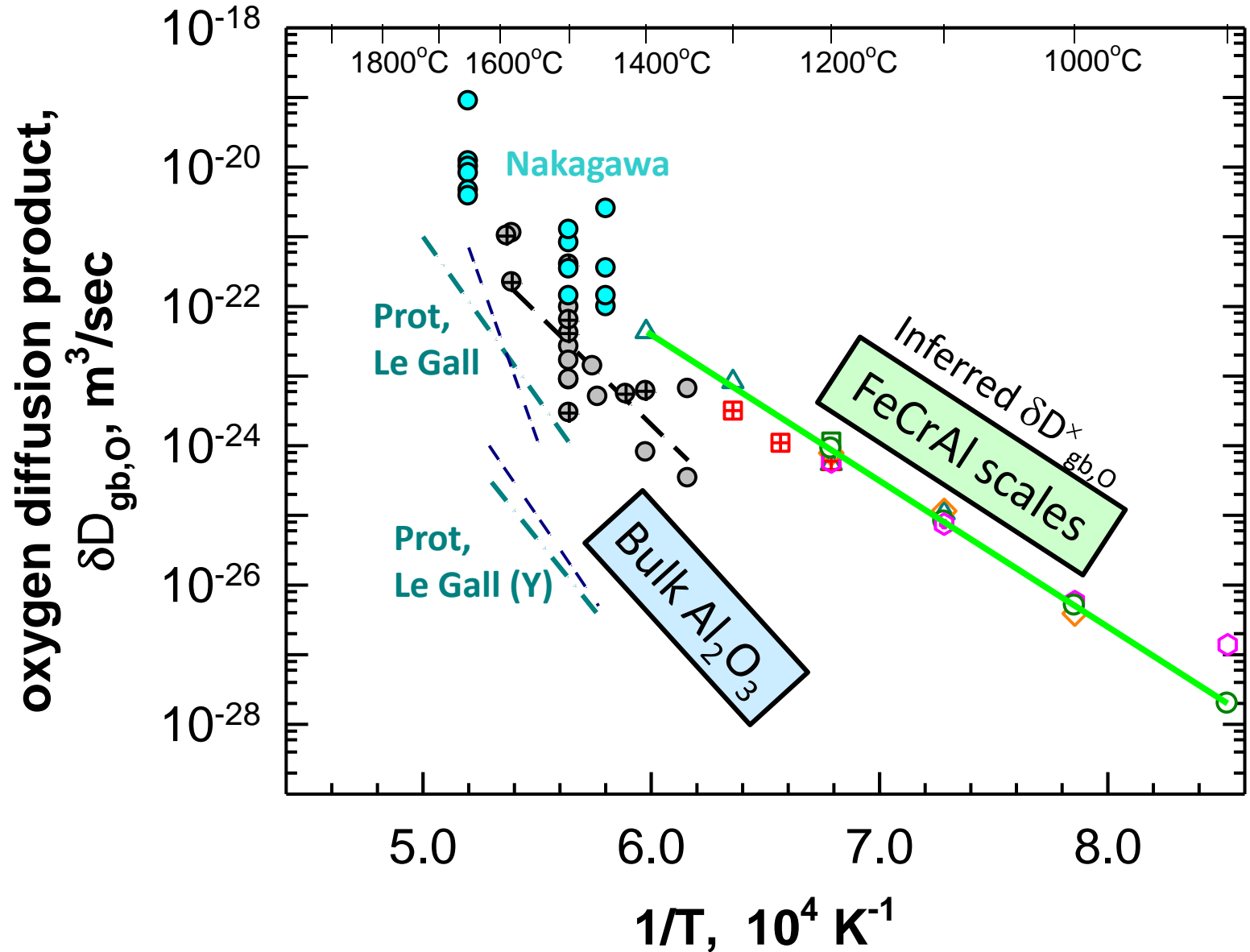
# Alumina Grain Boundary Diffusivity Product Bulk $^{18}\text{O}$ Tracer vs Permeability



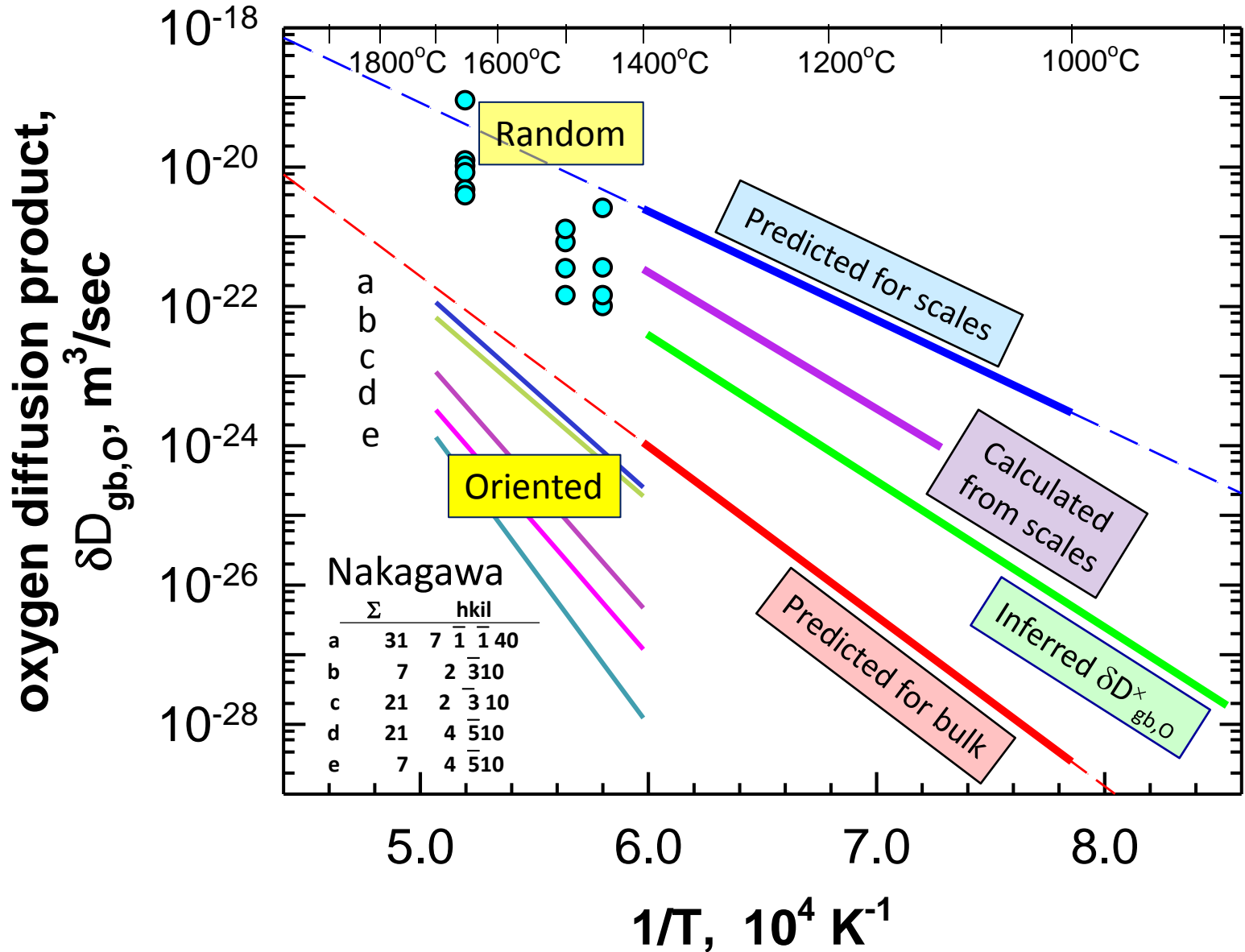
# Alumina Grain Boundary Diffusivity Product Bulk $^{18}\text{O}$ Tracer vs Permeability - Oxidation



# Alumina Grain Boundary Diffusivity Product Wagner Oxidation Compared to Bulk $^{18}\text{O}$ Tracer



# Alumina Grain Boundary Diffusivity Product Bicrystal $^{18}\text{O}$ Tracer vs Permeability/Oxidation



# Dopant Effects from Permeability Analyses

Matsudaira, Wada, Saitoh, Kitaoka

- Lu reduces  $\delta D_{gb}$  (oxygen) by 5x
- Hf reduces  $\delta D_{gb}$  (aluminum) by 3x
- Lu + Hf increase  $\delta D_{gb}$  (Al and oxygen) by 2x



# **Alumina Scale Growth Mechanisms: Some New Attractions from Permeability Analyses**

**Bulk values (1 atm) should not agree  
with scale values ( $10^{-33}$ - $10^{-23}$  atm):**

**Predicts  $\delta D_{\text{gb,O, scales}} \approx 10^4 \delta D_{\text{gb,O, bulk}}$**

# Alumina Scale Growth Mechanisms: Some New Attractions from Permeability Analyses

- Bulk  $\delta D_{gb}$  should **not** agree with scale;  $\delta D_{gb,O, scales} \approx 10^4 \delta D_{gb,O, bulk}$
- Interface (Oxygen):  $\delta D_{gb,O}$  and  $[V_O^{\circ\circ}] \propto (p_{O_2})^{-1/6}$
- Gas surface (Aluminum):  $\delta D_{gb,Al}$  and  $[V_{Al}'''] \propto (p_{O_2})^{+3/16}$
- $\delta D_{gb,O} \gg \delta D_{gb,Al}$

## Alumina Scale Growth Mechanisms: Some New Attractions from Permeability Analyses

- Bulk  $\delta D_{gb}$  should **not** agree with scale;  $\delta D_{gb,O, scales} \approx 10^4 \delta D_{gb,O, bulk}$
- Interface  $\delta D_{gb,O}, [V_O^{\bullet\bullet}] \propto p(O_{O_2})^{-1/6}$ ; Gas surface  $\delta D_{gb,Al}, [V_{Al}^{\bullet\bullet}] \propto p(O_{O_2})^{+3/16}$

**Oxidation Constant,  $\Pi$ , Gives Oxygen Diffusivity:**

$$\Pi_i = k_{p,i} \cdot G_i = 12 \delta D_{gb,O}$$

(and vice versa)

# Alumina Scale Growth Mechanisms: Some New Attractions from Permeability Analyses

- Bulk  $\delta D_{gb}$  should **not** agree with scale;  $\delta D_{gb,O, \text{scales}} \approx 10^4 \delta D_{gb,O, \text{bulk}}$
- Interface  $\delta D_{gb,O}, [V_O^{\circ\circ}] \propto p(O_{O_2})^{-1/6}$ ; Gas surface  $\delta D_{gb,Al}, [V_{Al}^{\circ\circ}] \propto p(O_{O_2})^{+3/16}$
- $\Pi_l = k_{p,i} \cdot G_i = 12 \delta D_{gb,O}$

$$Q_{\text{interface}} = Q_{1 \text{ atm}} + 1/n Q_{P(\text{equilibrium})}$$

$$298 = 467 - 1/6 (1012) \text{ kJ/mole}$$

$$375 = \text{measured from scales}$$

# Alumina Scale Growth Mechanisms: Some New Attractions from Permeability Analyses

- Bulk  $\delta D_{gb}$  should **not** agree with scale;  $\delta D_{gb,O, scales} \approx 10^4 \delta D_{gb,O, bulk}$
- Interface  $\delta D_{gb,O}, [V_O^{\circ\circ}] \propto p(O_{O_2})^{-1/6}$ ; Gas surface  $\delta D_{gb,Al}, [V_{Al}^{\circ\circ}] \propto p(O_{O_2})^{+3/16}$
- $\Pi_l = k_{p,i} \cdot G_i = 12 \delta D_{gb,O}$
- 298 kJ/mole predicted for scales; 375 kJ/mole measured for scales

## Highly Variable $\delta D_{gb,O}$ Bulk $^{18}O$ Measurements (Tsubasa Nakagawa, et al., U. Tokyo; CWRU)

$\delta D_{gb,O}$  (random) up to  $10^8 \delta D_{gb,O}$  (bicrystal)  
 $\Sigma 7, (4\bar{5}10)$  hkl

# Alumina Scale Growth Mechanisms: Some New Attractions from Permeability Analyses

- Bulk  $\delta D_{gb}$  should **not** agree with scale;  $\delta D_{gb,O, \text{ scales}} \approx 10^4 \delta D_{gb,O, \text{ bulk}}$
- Interface  $\delta D_{gb,O}, [V_O^{\circ\circ}] \propto p(O_{O_2})^{-1/6}$ ; Gas surface  $\delta D_{gb,Al}, [V_{Al}^{\circ\circ}] \propto p(O_{O_2})^{+3/16}$
- $\Pi_l = k_{p,i} \cdot G_i = 12 \delta D_{gb,O}$
- 298 kJ/mole predicted for scales; 375 kJ/mole measured for scales
- $\delta D_{gb,O} (\text{random}) = 10^8 \delta D_{gb,O}, \Sigma 7, (4\bar{5}10) \text{ hkil bicrystal}$